

GA design of wire pre-fractal antennas and comparison with other euclidean geometries

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Abstract— A multi-objective Genetic Algorithm (GA) tool has been applied in conjunction with the numerical electromagnetic code (NEC) to the optimization of wire pre-fractal Koch-like antennas in terms of bandwidth, efficiency and electrical size. The performance of the genetically engineered pre-fractal antennas is compared to that of other non-fractal wire geometries also designed by GA.

Index Terms—Genetic Algorithms, fractal antennas, wire antennas.

I. INTRODUCTION

THE design of electrically small antennas is a topic of current interest connected with the growing development of mobile-communication devices that require their components to be ever smaller and lighter.

As reducing the electrical size of an antenna is at the expense of other parameters such as bandwidth and efficiency [1], antenna miniaturization techniques require a compromise between all the parameters involved. This fact makes optimization techniques such as Genetic Algorithms (GA) a very appropriate tool for the design of such antennas. With this aim several authors have recently applied GA methods, for example Altshuler [2] who found a wire resonant antenna presenting a maximum bandwidth for a given antenna size, and Choo et al. [3] who applied a multi-objective version of GA to design small wire antennas taking into account bandwidth and efficiency.

Fractal shaped antennas, or more precisely pre-fractal geometries that are built with a finite number of iterations, due to their intricate and convoluted configurations, have been investigated by a number of authors as electrically small antennas [4]. GA techniques have also been applied to the design of pre-fractal antenna elements. For example a GA-engineered second-order Koch-like dual antenna having a compact size and low VSWR is presented in [5].

In this communication we extend the work in [5] to the

design, using a multiobjective GA, of wire pre-fractal Koch-like antennas, seeking an optimum set of solutions in terms of resonance frequency, bandwidth and efficiency. Moreover the GA code is employed to search for non-fractal structures, namely zig-zag and meander type antennas, and the resulting optimized solutions are compared to those obtained when the search space is restricted to pre-fractal Koch-like elements. It is shown that for a given overall wire length and antenna size, GA find euclidean-geometry designs that perform better than their pre-fractal counterparts. These results are in consonance with the analysis presented in [6] where the pre-fractal Hilbert wire antenna is shown to be less effective in lowering the resonance frequency than other non-fractal curves of the same size and length. In our case, the use of a multi-objective GA permits a thorough search of possible designs fulfilling all the specifications and their comparison in terms of more parameters than just the resonance frequency.

The paper is organized by first explaining in Section II the specific way in which GA is applied for the design of Koch-like wire antennas and other euclidean geometries. The results obtained are given in Section III.

II. GA DESIGN

A. Design of pre-fractal antennas

An Iterated Function System (IFS) algorithm [5] is applied to generate the shape of the pre-fractal antenna elements to be considered as individuals in the initial GA population. An IFS is a superposition of affine transformations characterized by a finite number of parameters. Examples of generating a Koch curve by means of an IFS can be found in [5, 7]. Fig. 1a shows an example of the kind of generating antennas considered in this paper, characterized by the parameters s_1 , s_2 , s_4 , s_5 , θ_2 , and θ_4 while Fig. 1b plots the resulting shape after the third order iteration of the IFS procedure.

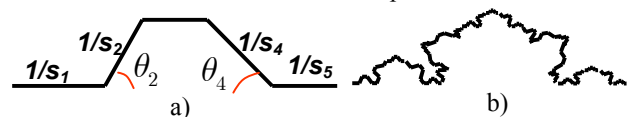


Fig. 1. Geometry of the generating antenna and its third order iteration.

A Pareto GA tool [8] has been developed to optimize several characteristics of the pre-fractal wire antennas simultaneously. In the GA code, the parameters s_1 , s_2 , s_4 , s_5 , θ_2 , θ_4 , which together with the number of iterations define a

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specific individual, are encoded into a chromosome. Instead of binary coding, fixed point decimal coding has been chosen [8] to gain a better definition of the search space with a minimum computational cost. A set of monopole antennas that constitute the initial generation are randomly formed. They are fed at their base, and their input impedance and resonance frequency are calculated applying the frequency-domain method-of-moments-based NEC code. To measure the goodness of a given individual and to permit the algorithm to evolve toward an optimal design, the following three fitness functions are defined:

$$F_i^1 = 1 - L_i; \quad F_i^2 = \frac{BW_i}{\Delta f}; \quad F_i^3 = 1 - \frac{f_{r,i}}{f_r^s} \quad (1)$$

where L_i is the length of the stretched wire corresponding to antenna i , BW_i the 2:1 SWR bandwidth, Δf the frequency range of interest, $f_{r,i}$ the resonance frequency of antenna i and f_r^s the resonance frequency of a straight monopole of length h . Our aim is to maximize F^1 and therefore minimize the ohmic losses that are related to length, F^2 so that a maximum bandwidth is achieved and F^3 so that for a given size of the antenna its resonance frequency is the smallest possible and therefore so is its electrical size at resonance. The joint maximization of the three parameters in (1) contributes to obtaining individuals with a low Q factor and a maximum efficiency. In order to avoid convergence to impractical individuals, constraints are also incorporated into the fitness functions and a penalty [9] is imposed on those individuals that, while not unfeasible as generating antennas, would be impossible to realize at a higher order. If the generating antenna is itself unfeasible a death penalty is applied and that individual is rejected. Any antenna is also restricted to fit in a given rectangle of dimensions $h \times w$, w being the width of a Koch curve of height h .

After applying the GA operators [8] of tournament method, one point crossover and a Gaussian-probability-distribution mutation, the multi-objective GA procedure renders a front or surface of optimal solutions (Pareto front) from which the designer can select the individual that best fits the requirements of the problem at hand. The procedure is applied by means of domination schemes using triangular sharing functions to guarantee diversity in the final set of optimal solutions [8].

B. Euclidean antennas

In order to investigate whether fractal shapes might be the best alternative for the design of efficient antennas with minimum resonance frequency, we have also allowed our GA code to look for euclidean geometries. In particular, zig-zag and meander type monopole antennas have been considered. They are built as explained below.

We start by restricting the space to be filled by the monopole antennas to the rectangle of dimensions $h \times w$ as in the Koch-like pre-fractal antennas described in the previous section. The geometry of a euclidean antenna is randomly

built by the GA code as a collection of consecutively connected straight segments starting at the feeding point. For a zig-zag type geometry, each segment j ($j = 1, \dots, N$) connects the end of the previous segment with a position of coordinates $y = j h / N$ and a randomly chosen value of x . A meander-type structure is built connecting N vertical segments and $N+1$ horizontal segments, each horizontal segment j ($j = 1, 3, \dots, 2N+1$) starts where $j-1$ ends and finishes at a random value of x and at $y = (j-1) h / (2N)$ (this may results is segments of zero length which are discarded at the end of the process). The N vertical segments of length h / N are joining the $j-1$ to the $j+1$ segment. An example of a zig-zag and a meander-type antenna with $N=14$, formed respectively by 14 and 24 segments, is shown in Fig. 2 together with their corresponding 14-bit decimal-coded chromosomes.

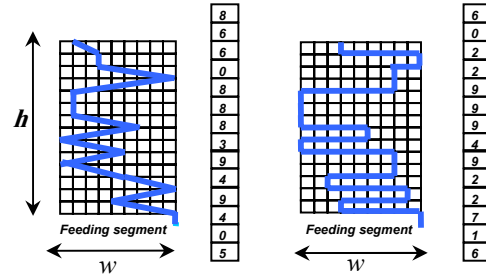


Fig. 2 Example of a zig-zag and a meander type antenna.

III. RESULTS

The specific GA adopted in this work employs both a crossover operator and a mutation operator with probabilities 80% and 5%, respectively. The population is formed with 20 chromosomes, comprising a set of $N=12$ genes which represent coded versions of the individual characteristics.

We begin by designing several wire antennas optimizing with GA only one at a time of the cost functions given in eq. (1). In all cases the possible antenna designs are restricted to the rectangle of height $h=6.22\text{cm}$ and width $w=1.73\text{cm}$. euclidean geometries are formed by 12 (zig-zag) or 24 (meander) wire segments ($N = 12$) and Koch-like antennas are considered up to second order. The best solution in terms of minimum length was the straight wire monopole of length 6.22cm . The same monopole was again found by GA when maximum bandwidth was requested. These are logical results that help to validate our GA code and that were obtained irrespective of whether the GA code was allowed to search for euclidean or Koch-like solutions. Regarding minimum resonance frequency (maximum F^3), Figure 3 shows the optimum second-order Koch-like solution (Fig. 3a), the zig-zag type solution (Fig. 3b) and the meander-type solution (Fig. 3c). The total length, L , the resonance frequency, f_r , and the BW of these antennas are given in the figure caption. Note that the antenna having minimum f_r (the meander) presents poor bandwidth and high length while the pre-fractal design having lowest ohmic losses and widest BW, has a

worse f_r than both euclidean designs. This is clearly a problem for which a multi-objective GA is needed in order to seek a compromise between the different parameters and to compare different designs under the same conditions.

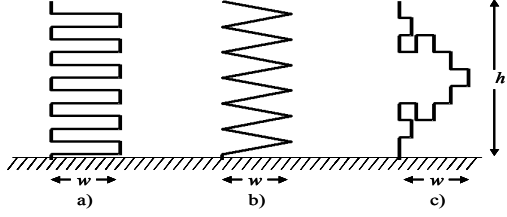


Fig. 3. a) Meander type antenna $L=26.97\text{cm}$, $f_r=449.8\text{ MHz}$, $BW=164\text{MHz}$. b) Zig-zag type antenna $L=22.01\text{cm}$, $f_r=559\text{MHz}$, $BW=222\text{MHz}$. c) Koch-like antenna $L=15.52\text{cm}$, $f_r=665.5\text{MHz}$, $BW=276.3\text{MHz}$.

Next, multi-objective optimization is considered in which we seek antennas, either second-order Koch-like or euclidean, that, fitting in the rectangle $6.22\text{cm} \times 1.73\text{cm}$, present minimum resonance frequency and length. Fig. 4 shows, with dot symbols, a plot of resonance frequency versus length for each individual and each iteration of the GA process for the case of a Koch-like design after 350 generations. As GA progresses, the envelope of the graph evolves to an optimal set of solutions, called the Pareto front, which is shown as a dashed line in Figure 4 and corresponds to the result after 2000 generations. Figure 5 also includes the Pareto front of optimal solutions in terms of length and resonance frequency for the cases of zig-zag and meander type antennas. The first and second iterations of a Koch monopole are also plotted for reference. It can be seen that euclidean geometries seem to perform better than the pre-fractal designs in reducing f_r given that for most of the possible lengths they render resonance frequencies that are smaller than those of their pre-fractal counterparts. Just at very low values of L all the antennas present a similar behaviour, but it should be mentioned that the optimization process did not provide enough number of individuals in this specific range of length for the results to be significant. For lengths higher than 10.5cm , meander antennas seem to be the electrically smallest choice. It should be pointed out that, although, to minimize computational resources, we did not search for greater lengths or pre-fractal orders, the results in Fig. 5 show that the distance between the Pareto fronts corresponding to Euclidean and pre-fractal designs increases with length, presenting the Euclidean antennas lower values of f_r .

Next, the bandwidth and length are considered. Fig. 6 shows the Pareto fronts corresponding to second-order pre-fractal, zig-zag and meander type antennas when the optimized parameters are F^1 and F^2 . Again the Koch 1 and 2 results have been marked for comparison. Note that both the meander and the zig-zag type show a better performance in terms of BW than the pre-fractal structures since, for a given length, they present the widest BW, the zig-zag type antennas always being the best choice.

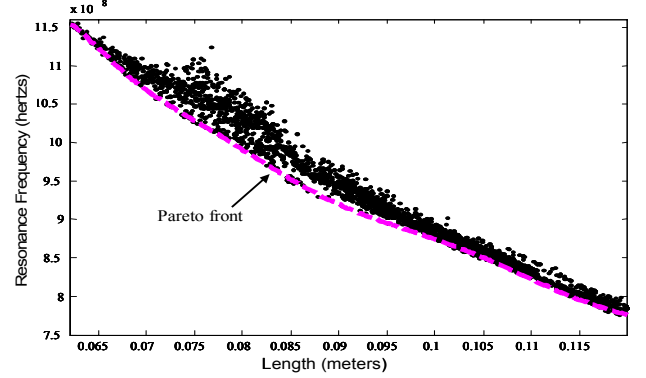


Fig. 4: Resonance frequency versus length of each Koch-like antenna at each iteration of the GA process. Dashed line: Pareto front.

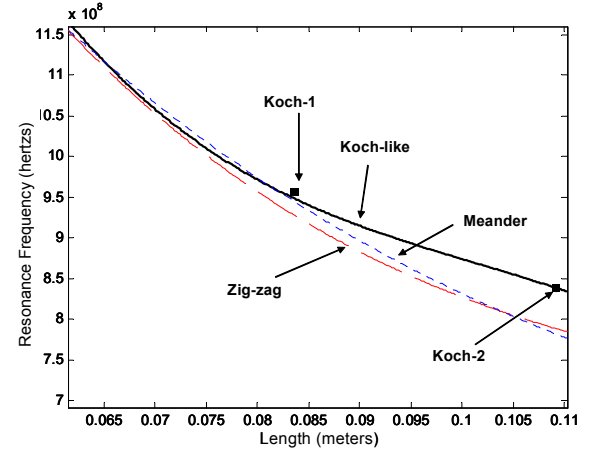


Fig. 5: Pareto fronts for the meander, zig-zag and Koch-like cases when optimizing F^1 and F^3

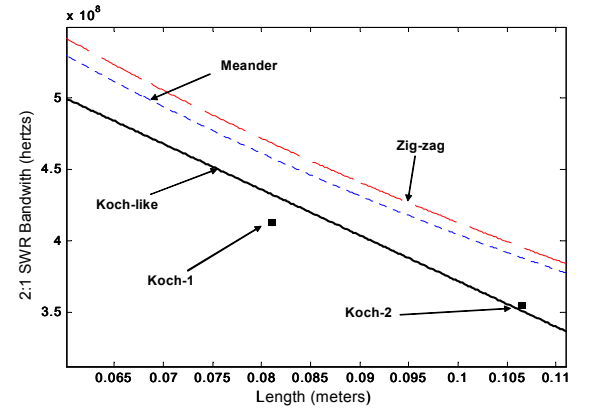


Fig. 6 Pareto fronts for the meander, zig-zag and Koch-like cases when the parameters optimized are F^1 and F^2

Finally the three fitness functions (1) have been optimized at the same time, seeking an antenna design fitting in the same rectangle as in the previous examples. Now the Pareto fronts are the surfaces shown in Figure 7. The squared and crossed symbols represent the zig-zag and meander type solutions respectively while Koch-like solutions are shown as a continuous surface. From that figure, the designer can choose the antenna elements that best fit the specified requirements of the problem at hand. In particular we have selected the three individuals plotted in Figure 8, all of them

having approximately the same length ($L \simeq 10.22$ cm) and radius of 0.1 mm. Their resonance frequencies, f_r , Q factor, bandwidth and efficiency, η , have been calculated with NEC and are given in Table I. Experimental results are obtained when the antennas are modelled as copper strips (0.29mm width and 25 μ m thick) printed on a 0.25mm thick fiberglass FR4. The dimensions of the strip are chosen so the actual geometry where the current flows in the strip has the same cross section surface as when it flows in the original wire. The measured data are given in Table II and show a reasonable agreement with the numerical experiments confirming that the non-fractal antennas, either zig-zag or meander, perform better than the fractal designs. The slight differences between measurements and numerical data can be attributed to the two different models considered for the antennas. The measurements of the efficiency and the Q factor have been carried out following the methods described in [10] and [11] respectively.

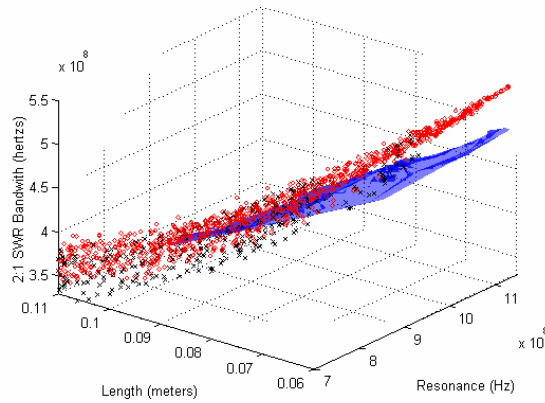


Figure 7: Pareto surfaces when optimizing F^1 , F^2 and F^3

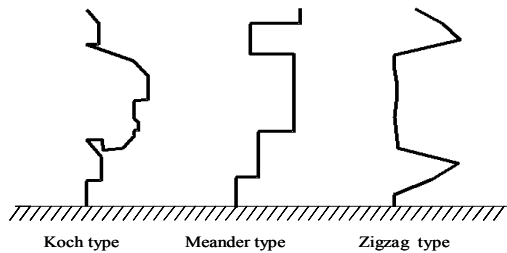


Figure 8: Geometry of the three antennas selected from Fig. 7

Antenna	f_r (MHz)	Q	η (%)	BW (MHz)
Koch	864.5	13.57	96.8	365.4
Meander	826.5	12.67	97.19	346.3
Zig-zag	824	13.99	96.79	330.6

Table I: Parameters antennas in Fig. 8 calculated numerically.

	f_r (MHz)	Q	η (%)
Koch	905	12.67	87.64
Meander	850	12.60	88.78
Zig-zag	870	13.89	87.34

Table II: Experimental results for the antennas in Fig. 8.

IV. CONCLUSIONS

A multi-objective GA algorithm has been applied to the design of wire antennas optimizing their bandwidth and efficiency while reducing their resonance frequency. Second-order Koch-like pre-fractal antennas have been considered as well as other euclidean geometries such as zig-zag and meander type antennas. The performance of the non-fractal curves was always better than that of the Koch-like structures. In particular, for a given antenna size and length, the non-fractal designs usually present a lower resonance frequency and wider bandwidth, resulting in a lower Q factor and higher efficiency.

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